AMC 10

2005

	В
1	a price of two for \$1. What was their prot, in dollars?
2	 (A) 100 (B) 200 (C) 300 (D) 400 (E) 500 A positive number x has the property that x% of x is 4. What is x? (A) 2 (B) 4 (C) 10 (D) 20 (E) 40
3	A gallon of paint is used to paint a room. One third of the paint is used on the first day. On the second day, one third of the remaining paint is used. What fraction of the original amount of paint is available to use on the third day?
4	(A) $\frac{1}{10}$ (B) $\frac{1}{9}$ (C) $\frac{1}{3}$ (D) $\frac{4}{9}$ (E) $\frac{5}{9}$ For real numbers a and b , define $a \diamond b = \sqrt{a^2 + b^2}$. What is the value of $(5 \diamond 12) \diamond ((-12) \diamond (-5))$?
	(A) 0 (B) $\frac{17}{2}$ (C) 13 (D) $13\sqrt{2}$ (E) 26
5	Brianna is using part of the money she earned on her weekend job to buy several equally-priced CDs. She used one fifth of her money to buy one third of the CDs. What fraction of her money will she have left after she buys all the CDs? (A) $\frac{1}{5}$ (B) $\frac{1}{3}$ (C) $\frac{2}{5}$ (D) $\frac{2}{3}$ (E) $\frac{4}{5}$
6	At the beginning of the school year, Lisas goal was to earn an A on at least 80% of her 50 quizzes for the year. She earned an A on 22 of the first 30 quizzes. If she is to achieve her goal, on at most how many of the remaining quizzes can she earn a grade lower than an A? (A) 1 (B) 2 (C) 3 (D) 4 (E) 5
7	A circle is inscribed in a square, then a square is inscribed in this circle, and finally, a circle is inscribed in this square. What is the ratio of the area of the smaller circle to the area of the larger square?
	(A) $\frac{\pi}{16}$ (B) $\frac{\pi}{8}$ (C) $\frac{3\pi}{16}$ (D) $\frac{\pi}{4}$ (E) $\frac{\pi}{2}$
8	An 8-foot by 10-foot floor is tiled with square tiles of size 1 foot by 1 foot. Each tile has a pattern consisting of four white quarter circles of radius 1/2 foot centered at each corner of the tile. The remaining portion of the tile is shaded. How many square feet of the floor are shaded?

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(A)
$$80 - 20\pi$$

(B)
$$60 - 10\pi$$

(C)
$$80 - 10\pi$$

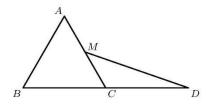
(D)
$$60 + 10\pi$$

(E)
$$80 + 10\pi$$

- 9 One fair die has faces 1, 1, 2, 2, 3, 3 and another has faces 4, 4, 5, 5, 6, 6. The dice are rolled and the numbers on the top faces are added. What is the probability that the sum will be odd?
 - (A) $\frac{1}{3}$

- (B) $\frac{4}{9}$ (C) $\frac{1}{2}$ (D) $\frac{5}{9}$ (E) $\frac{2}{3}$
- 10 In $\triangle ABC$, we have AC = BC = 7 and AB = 2. Suppose that D is a point on line AB such that B lies between A and D and CD = 8. What is BD?
 - (A) 3
- **(B)** $2\sqrt{3}$
- (C) 4
- (D) 5
- (E) $4\sqrt{2}$
- 11 The first term of a sequence is 2005. Each succeeding term is the sum of the cubes of the digits of the previous terms. What is the 2005th term of the sequence?
 - (A) 29
- (B) 55
- (C) 85
- (D) 133
- (E) 250
- [12] Twelve fair dice are rolled. What is the probability that the product of the numbers on the top faces is prime?
 - (A) $\left(\frac{1}{12}\right)^{12}$

- **(B)** $\left(\frac{1}{6}\right)^{12}$ **(C)** $2\left(\frac{1}{6}\right)^{11}$ **(D)** $\frac{5}{2}\left(\frac{1}{6}\right)^{11}$ **(E)** $\left(\frac{1}{6}\right)^{10}$
- 13 How many numbers between 1 and 2005 are integer multiples of 3 or 4 but not 12?
 - (A) 501
- (B) 668
- (C) 835
- (D) 1002
- (E) 1169
- 14 Equilateral $\triangle ABC$ has side length 2, M is the midpoint of \overline{AC} , and C is the midpoint of \overline{BD} . What is the area of $\triangle CDM$?



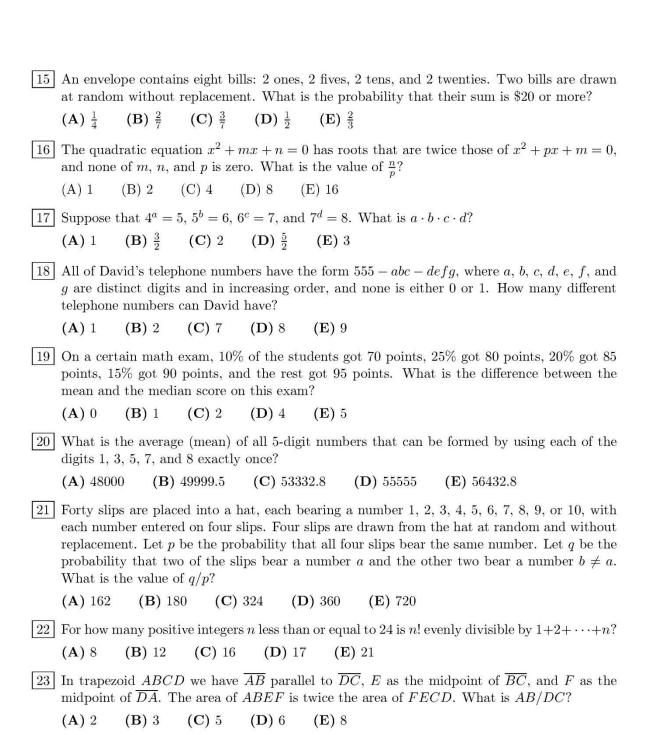
- (A) $\frac{\sqrt{2}}{2}$ (B) $\frac{3}{4}$
- (C) $\frac{\sqrt{3}}{2}$
- **(D)** 1
- (E) $\sqrt{2}$

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- Let x and y be two-digit integers such that y is obtained by reversing the digits of x. The integers x and y satisfy $x^2 y^2 = m^2$ for some positive integer m. What is x + y + m?
 - (A) 88
- **(B)** 112
- (C) 116
- **(D)** 144
- **(E)** 154
- 25 A subset B of the set of integers from 1 to 100, inclusive, has the property that no two elements of B sum to 125. What is the maximum possible number of elements in B?
 - (A) 50
- **(B)** 51
- (C) 62
- **(D)** 65
- (E) 68

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2005 AMC 10B Answer Key

- 1. A
- 2. D
- 3. D
- 4. D
- 5. C
- 6. B
- 7. B
- 8. A
- 9. D
- 10.A
- 11.E
- 12.E
- 13.C
- 14.C
- 15.D
- 16.D
- 17.B
- 18.D
- 19.B
- 20.C
- 21.A
- 22.C
- 23.C
- 24.E
- 25.C

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